

WRITTEN METHODS:

By the end of year 6, children will have a **range** of mental calculation methods and the **one** reliable written method shown in this progression.

Selection will depend on the numbers involved.

Children should not be made to go on to the next stage if:

- 1) they are not ready
 - 2) they are not confident
- Children should be encouraged to approximate their answers before calculating.
 - Children should be encouraged to check their answers after the calculation using an appropriate strategy.
 - Children should be encouraged to consider if a mental calculation would be appropriate before using written methods.

Children should be encouraged to select an appropriate calculation method, be it mental or written, dependent on the numbers involved in a calculation. To develop this skill children should be taught to ask themselves, '**Can I do this mentally?**'

INFORMAL EXPANDED METHOD: This leads the children to the more compact standard written method, developing an understanding of its structure and efficiency.

$$\begin{array}{ccc} 98 \div 7 = 14 \\ \swarrow \quad \downarrow \quad \searrow \\ \text{dividend} \quad \text{divisor} \quad \text{quotient} \end{array}$$

The teacher should model using the correct language and encourage children to use it, e.g.

dividend, divisor, quotient

Progression for Written Division

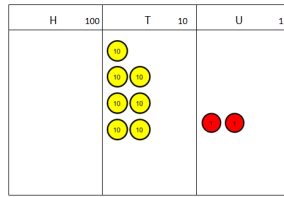
INFORMAL EXPANDED WRITTEN METHOD USING EFFICIENT CHUNKING:

Encourage children to produce a 'FACTS LIST' using their knowledge of place value and related facts, looking for the two multiples of ten that 'TRAP' the dividend. They should be encouraged to find the largest possible multiple of ten of the divisor and what's left.

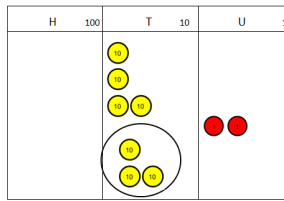
Short Division

Encourage children to develop the skill of 'trapping' the dividend to prepare for partitioning.

TU ÷ U 72 ÷ 3



10 X 3 = 30



Facts list 72 ÷ 3

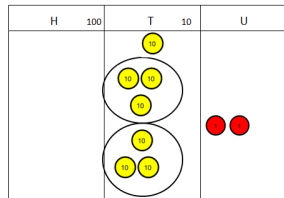
10 x 3 = 30

20 x 3 = 60

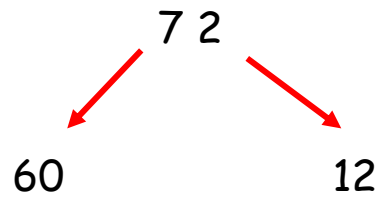
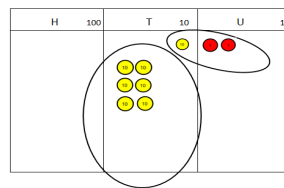
30 x 3 = 90

← 72
'Trap the dividend'

20 X 3 = 60



72 partitioned into -



72 ÷ 3

60 ÷ 3 = 20

12 ÷ 3 = 4

= 24

TU
4
20
3 | 72
- 60

12
- 12

0

Notes

Progression for Written Division

When children are confident using the Facts List and efficient chunking for short division with understanding, along with increased times table knowledge and without needing PV counters, move on to division using larger numbers.

HTU ÷ U

$$\begin{array}{r}
 \text{HTU} \\
 35 \\
 7 \overline{) 247} \\
 \underline{-210} \\
 37 \\
 \underline{-35} \\
 2
 \end{array}$$

Facts list

10 x 7 = 70

20 x 7 = 140

30 x 7 = 210

40 x 7 = 280

247
 ← 'Trap the dividend'

$247 \div 7 = 35 \text{ r}2 \text{ or } \frac{2}{7}$

$$\frac{2}{7}$$



2 left out of
 a group of 7
 which equals
 $\frac{2}{7}$

Notes

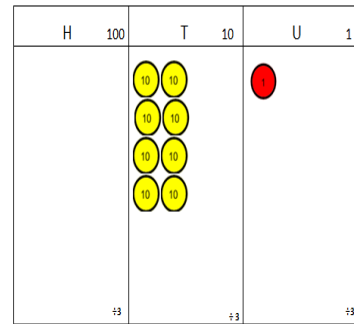
Progression for Written Division

COMPACT METHOD:

Short Division: TU/HTU/ THTU ÷ U

Those children who are confident and efficient working with the expanded method could be taught the more compact method of short division leading into dividing with decimals.

Facts List
 TU ÷ U 10 × 3 = 30
 81 ÷ 20 × 3 = 60 ← 81 Trap the dividend
 30 × 3 = 90



There are 20 lots of 3 in 60

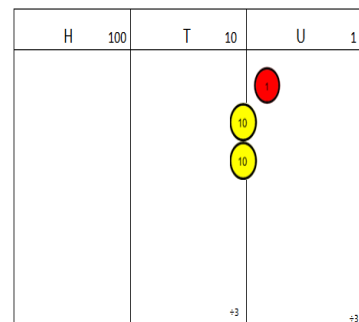
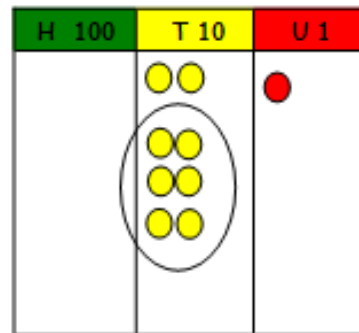
There are 2 tens and 1 unit left over

Children will then mentally work out that there are 7 groups of 3 in 21.

There are 7 lots of 3 in 21 units

$$\begin{array}{r} \text{HTU} \\ 7 \\ 20 \\ 3 \overline{) 81} \end{array}$$

81 ÷ 3 = 27



Notes

Progression for Written Division

HTU ÷ U

291 ÷ 3

Facts List

50 x 3 = 150

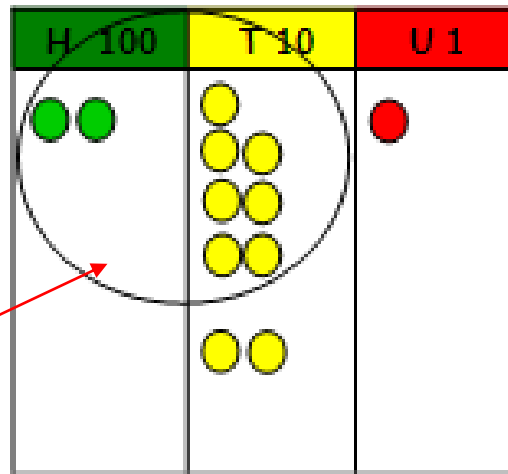
60 x 3 = 180

70 x 3 = 210

80 x 3 = 240

90 x 3 = 270 ← 291 Trap the dividend

100 x 3 = 300



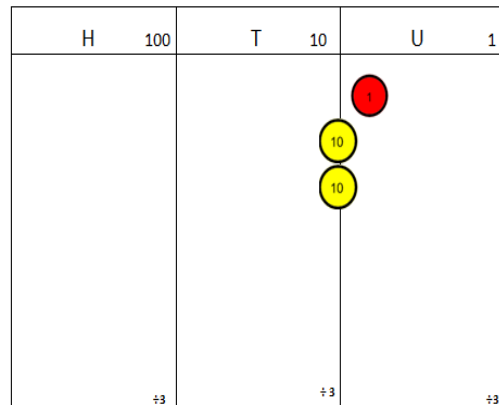
90 lots of 3 = 270

$$\begin{array}{r} \text{HTU} \\ 90 \\ \hline 3 \overline{) 291} \end{array}$$

There are 2 tens and 1 unit left over

Children will then mentally work out that there are 7 groups of 3 in 21.

$$\begin{array}{r} \text{HTU} \\ 97 \\ \hline 3 \overline{) 291} \end{array}$$



291 ÷ 3 = 97

Develop short division up to 4 digit and involving decimals interpreting remainders appropriately according to the context.

Points to Consider

- Practical problem solving should continue throughout Key Stages 1 and 2 using division.
- When calculating with decimals and demonstrating understanding scale up by multiplying by 10 or 100, depending on the number of decimal places; and scale down by the same to give the answer.

E.g. $87.5 \div 7$ $\xrightarrow{\text{scale up by 10}}$ $87.5 \times 10 = 875$ $\xrightarrow{\quad}$ $875 \div 7$

$$\begin{array}{r} 125 \\ 7 \overline{) 875} \\ \underline{7} \\ 17 \\ \underline{14} \\ 35 \\ \underline{35} \\ 0 \end{array}$$

Scale down by 10 $\longrightarrow 125 \div 10 = 12.5$

$$87.5 \div 7 = 12.5$$

Long division HTU \div TU

$$603 \div 26$$

$$603 \div 26 = 23 \text{ r}5$$

Facts List

$$10 \times 26 = 260$$

$$20 \times 26 = 520$$

$$30 \times 26 = 780$$

\longleftarrow 603 Trap the dividend

$$\begin{array}{r} \text{HTU} \\ 23 \\ 26 \overline{) 603} \\ \underline{- 520} \\ 83 \\ \underline{- 78} \\ 5 \end{array}$$

r5 or 5/26 depending on the context